

Priprema za ispit znanja – Trigonometrijske jednačbe i nejednačbe – RM 18

1. $2\sin^2 x + 2 = 5\sin x$

Rj: $x_1 = \frac{\pi}{6} + 2k\pi, x_2 = \frac{5\pi}{6} + 2k\pi, k \in \mathbb{Z}$

2. $4\sin^2 x + \sin x \cos x + \cos^2 x = 3$

Rj: $x_1 = -63^\circ 26' 6'' + k \cdot 180^\circ, x_2 = \frac{\pi}{4} + k\pi, k \in \mathbb{Z}$

3. $4\cos^2 x = 1 + 4\sin x$

Rj: $x_1 = \frac{\pi}{6} + 2k\pi, x_2 = \frac{5\pi}{6} + 2k\pi, k \in \mathbb{Z}$

4. $3\sin x + \sqrt{3}\cos x = 0$

Rj: $x_1 = -\frac{\pi}{6} + k\pi, k \in \mathbb{Z}$



5. $\sin 2x = \cos^2 x$

Rj: $x_1 = 26^\circ 33' 54'' + k \cdot 180^\circ, k \in \mathbb{Z}$

6. $\sin 2x + 2\cos x = 1 + \sin x$

Rj: $x_1 = -\frac{\pi}{2} + 2k\pi, x_{2,3} = \pm \frac{\pi}{3} + 2k\pi, k \in \mathbb{Z}$

7. $\sin\left(x + \frac{\pi}{6}\right) + \cos\left(\frac{\pi}{3} + x\right) = 1 + \cos 2x$

Rj: $x_1 = \frac{\pi}{2} + k\pi, x_2 = \pm \frac{\pi}{3} + 2k\pi, k \in \mathbb{Z}$

8. $\sin x \cos 4x = \sin 5x$

Rj: $x_1 = \frac{\pi}{2} + k\pi, x_2 = \frac{k\pi}{4}, k \in \mathbb{Z}$

9. $\sin x + \sin 3x + \sin 5x = 0$

Rj: $x_1 = \frac{k\pi}{3}, x_{2,3} = \pm \frac{\pi}{3} + k\pi, k \in \mathbb{Z}$

10. $\operatorname{tg}^2 3x - \operatorname{tg} 3x = 0$

Rj: $x_1 = \frac{k\pi}{3}, x_2 = \frac{\pi}{12} + \frac{k\pi}{3}, k \in \mathbb{Z}$

11. $\sin 7x = \sin 3x$

Rj: $x_1 = \frac{k\pi}{2}, x_2 = \frac{\pi}{10} + \frac{k\pi}{5}, k \in \mathbb{Z}$

12. $\sin^2 x + \sin^2 2x = 1$

Rj: $x_1 = \frac{\pi}{2} + k\pi, x_{2,3} = \pm \frac{\pi}{3} + k\pi, k \in \mathbb{Z}$

13. $\sin^2 x + 2\sin x \geq 0$

Rj: $2k\pi \leq x \leq \pi + 2k\pi, k \in \mathbb{Z}$

14. $2\cos^2 x + 3\cos x < -1$

Rj: $\frac{2\pi}{3} + 2k\pi < x < \frac{4\pi}{3} + 2k\pi \setminus \{\pi + 2k\pi\}, k \in \mathbb{Z}$

15. $8 - 3\operatorname{tg} 2x \geq 0$

Rj: $-45^\circ + k \cdot 90^\circ \leq x \leq 34^\circ 43' 19'' + k \cdot 90^\circ, k \in \mathbb{Z}$